GraphPrompt: Unifying Pre-Training and Downstream Tasks for Graph Neural Networks

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Code: https://github.com/Starlien95/GraphPrompt





Introduction

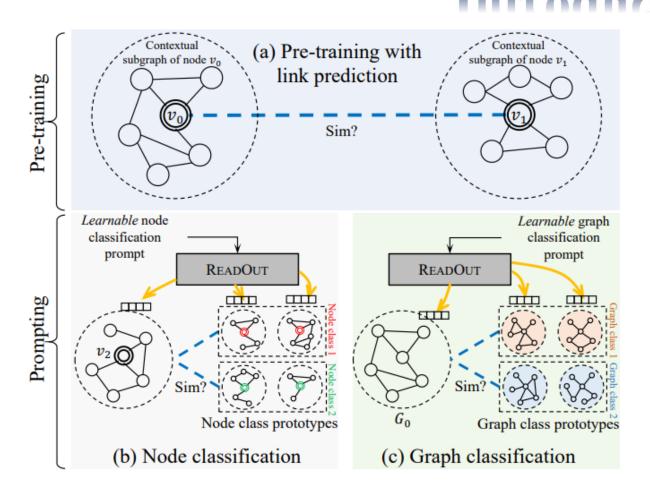


Figure 1: Illustration of the motivation. (a) Pre-training on graphs. (b/c) Downstream node/graph classification.

GraphPrompt unifies pre-training and downstream tasks into a common task template

However, existing study of prompting on graphs is still limited, lacking a universal treatment to appeal to different downstream task

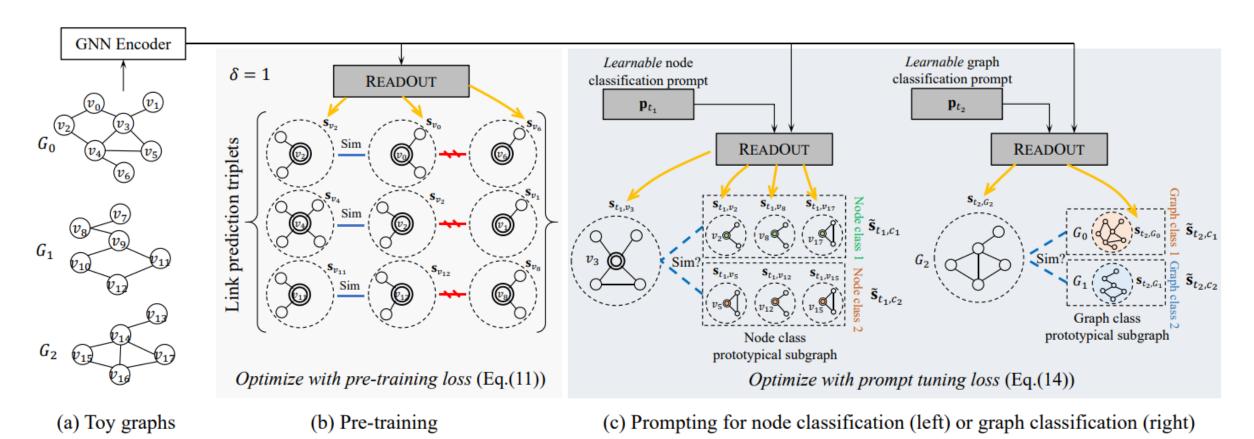
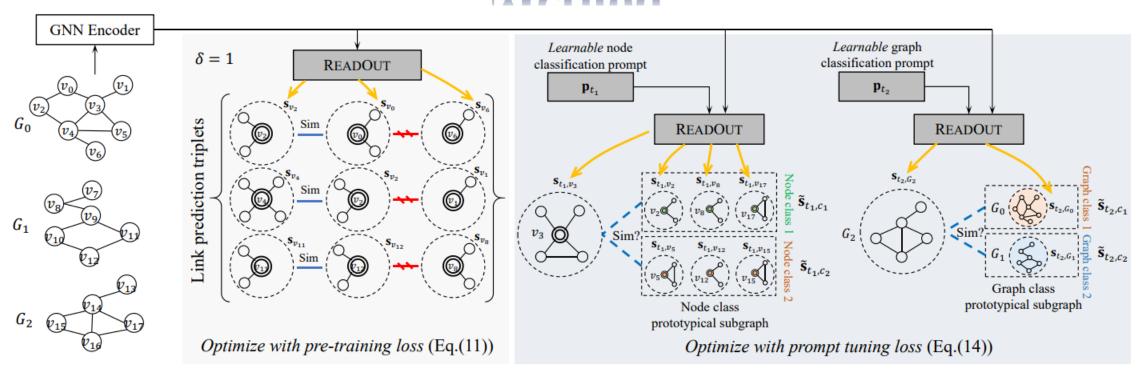


Figure 2: Overall framework of GRAPHPROMPT.



(a) Toy graphs

(b) Pre-training

(c) Prompting for node classification (left) or graph classification (right)

Figure 2: Overall framework of GRAPHPROMPT.

$$G = (V, E)$$

 $\mathbf{X} \in \mathbb{R}^{|V| \times d}$
 $\mathcal{G} = \{G_1, G_2, \dots, G_N\}$

k-shot classification

$$\ell_i \in C \quad G_i \in \mathcal{G}$$

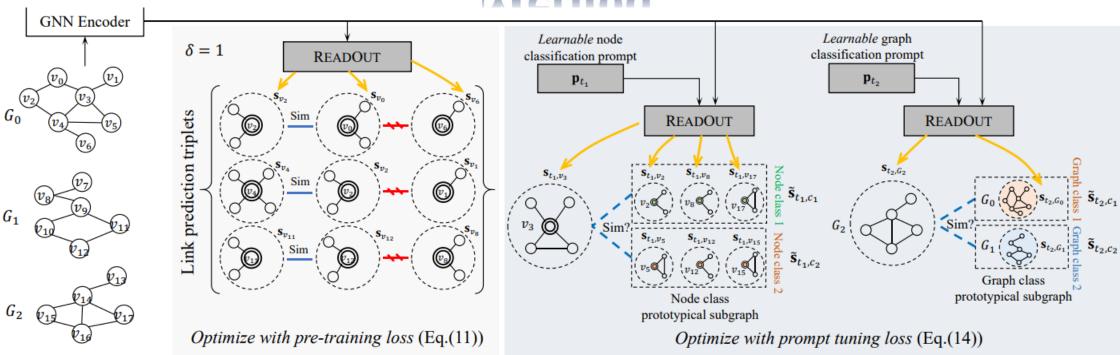
$$\mathbf{h}_v^l = \operatorname{Aggr}(\mathbf{h}_v^{l-1}, \{\mathbf{h}_u^{l-1} : u \in \mathcal{N}_v\}; \theta^l),$$

(1)
$$\Theta = \{\theta^1, \theta^2, \ldots\}$$

$$V(S_v) = \{d(u, v) \le \delta \mid u \in V\}, \text{ and }$$

$$\mathbf{h}_{v}$$

$$E(S_v) = \{(u, u') \in E \mid u \in V(S_v), u' \in V(S_v)\},$$
(3)



(a) Toy graphs

(b) Pre-training

$$sim(\mathbf{s}_v, \mathbf{s}_a) > sim(\mathbf{s}_v, \mathbf{s}_b). \tag{4}$$

$$\tilde{\mathbf{s}}_c = \frac{1}{k} \sum_{(v_i, \ell_i) \in D, \ell_i = c} \mathbf{s}_{v_i}. \tag{5}$$

$$\ell_j = \arg\max_{c \in C} \operatorname{sim}(\mathbf{s}_{v_j}, \tilde{\mathbf{s}}_c). \tag{6}$$

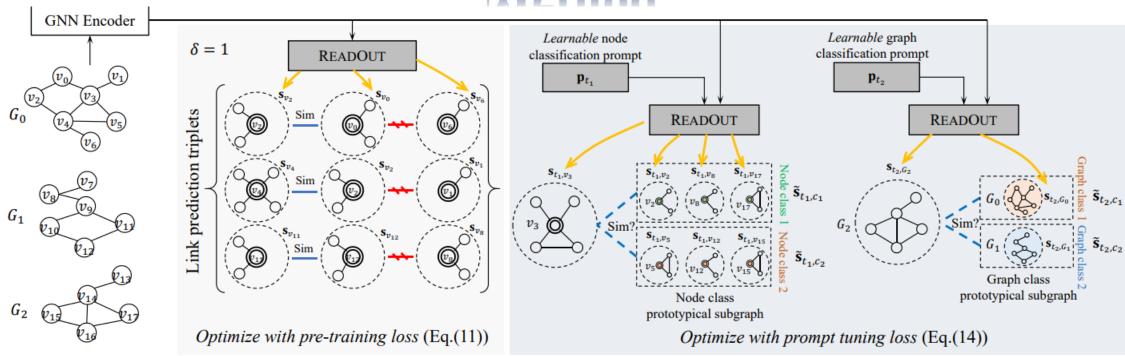
(c) Prompting for node classification (left) or graph classification (right)

$$\tilde{\mathbf{s}}_c = \frac{1}{k} \sum_{(G_i, L_i) \in \mathcal{D}, L_i = c} \mathbf{s}_{G_i}.$$
 (7)

$$L_j = \arg\max_{c \in C} \sin(\mathbf{s}_{G_j}, \tilde{\mathbf{s}}_c). \tag{8}$$

$$y = \arg\max_{c \in Y} \operatorname{sim}(\mathbf{s}_{x}, \tilde{\mathbf{s}}_{c}). \tag{9}$$

$$\mathbf{s}_{x} = \text{ReadOut}(\{\mathbf{h}_{v} : v \in V(S_{x})\}). \tag{10}$$



(a) Toy graphs

(b) Pre-training

$$\mathcal{L}_{\text{pre}}(\Theta) = -\sum_{(v,a,b)\in\mathcal{T}_{\text{pre}}} \ln \frac{\exp(\text{sim}(\mathbf{s}_v, \mathbf{s}_a)/\tau)}{\sum_{u\in\{a,b\}} \exp(\text{sim}(\mathbf{s}_v, \mathbf{s}_u)/\tau)}, \quad (11)$$

 $\Theta_0 = \arg\min_{\Theta} \mathcal{L}_{pre}(\Theta)$

$$\mathbf{s}_{t,x} = \text{ReadOut}(\{\mathbf{p}_t \odot \mathbf{h}_v : v \in V(S_x)\}), \tag{12}$$

(c) Prompting for node classification (left) or graph classification (right)

$$\mathbf{s}_{t,x} = \text{ReadOut}(\{\mathbf{P}_t \mathbf{h}_v : v \in V(S_x)\}). \tag{13}$$

$$\mathcal{L}_{\text{prompt}}(\mathbf{p}_t) = -\sum_{(x_i, y_i) \in \mathcal{T}_t} \ln \frac{\exp(\text{sim}(\mathbf{s}_{t, x_i}, \tilde{\mathbf{s}}_{t, y_i}) / \tau)}{\sum_{c \in Y} \exp(\text{sim}(\mathbf{s}_{t, x_i}, \tilde{\mathbf{s}}_{t, c}) / \tau)}, \quad (14)$$

Note that, the prompt tuning loss is only parameterized by the learnable prompt vector \mathbf{p}_t , without the GNN weights.

Table 1: Summary of datasets.

	Graphs	Graph classes	Avg. nodes	Avg. edges	Node features	Node classes	Task (N/G)
Flickr	1	-	89,250	899,756	500	7	N
PROTEINS	1,113	2	39.06	72.82	1	3	N, G
COX2	467	2	41.22	43.45	3	-	G
ENZYMES	600	6	32.63	62.14	18	3	N, G
BZR	405	2	35.75	38.36	3	-	G

Table 2: Accuracy evaluation on node classification.

All tabular results are in percent, with best **bolded** and runner-up <u>underlined</u>.

Methods	Flickr 50-shot	PROTEINS 1-shot	ENZYMES 1-shot	
GCN	9.22 ± 9.49	59.60 ± 12.44	61.49 ± 12.87	
GRAPHSAGE	13.52 ± 11.28	59.12 ± 12.14	61.81 ± 13.19	
GAT	16.02 ± 12.72	58.14 ± 12.05	60.77 ± 13.21	
GIN	10.18 ± 5.41	$\underline{60.53} \pm 12.19$	63.81 ± 11.28	
DGI	17.71 ± 1.09	54.92 ± 18.46	63.33 ± 18.13	
GRAPHCL	18.37 ± 1.72	52.00 ± 15.83	58.73 ± 16.47	
GPPT	18.95 ± 1.92	50.83 ± 16.56	53.79 ± 17.46	
GraphPrompt	20.21 ± 11.52	63.03 ± 12.14	67.04 ± 11.48	

Table 3: Accuracy evaluation on graph classification.

Methods	PROTEINS 5-shot	COX2 5-shot	ENZYMES 5-shot	BZR 5-shot	
GCN GRAPHSAGE GAT GIN	52.99 ± 10.57	51.37 ± 11.06 52.87 ± 11.46 51.20 ± 27.93 51.89 ± 8.71	18.31 ± 6.22	57.23 ± 10.95	
InfoGraph GraphCL GraphPrompt	$ \begin{vmatrix} 54.12 \pm 8.20 \\ 56.38 \pm 7.24 \end{vmatrix} $ $ 64.42 \pm 4.37 $	54.04 ± 9.45 55.40 ± 12.04 59.21 ± 6.82	28.11 ± 4.00	59.22 ± 7.42	

Table 4: Study of parameter efficiency on node classification.

Mathada	Flickr		PROTEINS		ENZYMES	
Methods	Params	FLOPs	Params	FLOPs	Params	FLOPs
GIN	22,183	240,100	5,730	12,380	6,280	11,030
GPPT	4,096	4,582	1,536	1,659	1,536	1,659
GRAPHPROMPT	96	96	96	96	96	96
GRAPHPROMPT-ft	21,600	235,200	6,176	13,440	6,176	10,944

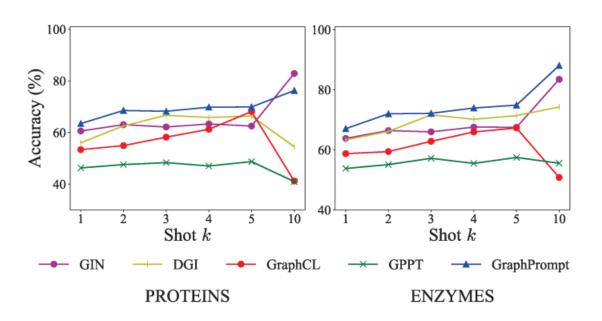


Figure 3: Impact of shots on few-shot node classification.

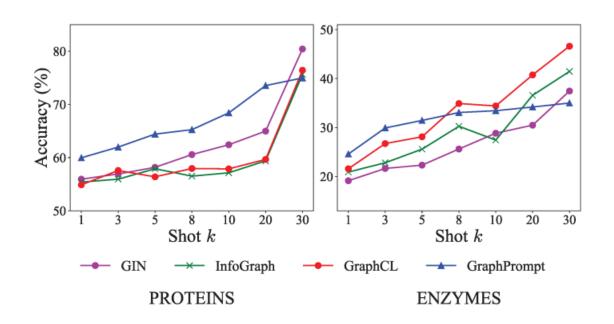


Figure 4: Impact of shots on few-shot graph classification.

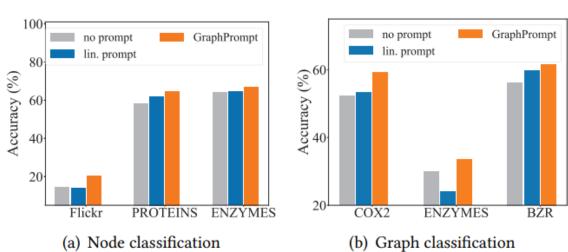


Figure 5: Ablation study.

Thanks